# Exergy(火用) or Availability <br> "Understanding engineering thermo" 

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To get true maximum available work, all the heat to be rejected from the system has to be rejected at the temperature of the surroundings.

- Similarly, if the system and surroundings are at different pressures and if the system expands, then to minimize the nonuseful pV work, the expansion should always be done at the pressure of the surroundings.
- The maximum extractable work depends on three quantities: the states of the system,1,2 and the state of the surroundings, 0 .
- This work concept was first mentioned by J.C. Maxwell in his "theory of Heat"
- To distinguish it from all other forms of work, Rant coined a new term "exergy", to represent this concept.


## EXERGY OF BATCH SYSTEM,

$\mathbf{W E X}_{\mathrm{EX}, \mathrm{Batch}}$

- $W_{\text {ex, } 1 \rightarrow 0, \text { batch }}$ : Consider a system at $T_{1}, p_{1}$ and having $E_{p 1}$ and $E_{k 1}$, while the surroundings are at $T_{0}, p_{0}$.

from Carnot engine, since $\frac{\left|Q_{0}\right|}{|Q|}=\frac{T_{0}}{T}, \frac{d\left|Q_{0}\right|}{d|Q|}=\frac{T_{0}}{T}$
given up by the system
then $\quad d\left|Q_{0}\right|=T_{0} \frac{d|Q|}{T}=T_{0} d S \longleftarrow$ of surroundings
- Consider a very small (differential) move of the system (at T, p) towards equilibrium. The total work produced,


$$
\mathrm{d}\left|\mathrm{Q}_{0}\right|=\mathrm{T}_{0} \frac{\mathrm{~d}|\mathrm{Q}|}{\mathrm{T}}=\mathrm{T}_{0} \mathrm{dS}
$$

from the $1^{\text {st }}$ law, $\mathrm{dE}=\mathrm{dQ}_{0}-\mathrm{dW}_{\text {total }}$
therefore, $\mathrm{dW}_{\mathrm{ex}}=\mathrm{dW}_{\mathrm{sh}}+\mathrm{dW}=-\mathrm{dE}+\mathrm{T}_{0} \mathrm{~S}-\mathrm{p}_{0} \mathrm{dv}$

- For the whole progression of changes for the system from $T_{1}$, $p_{1}, E_{p 1}, E_{k 1}$ to $T_{0}, p_{0}$ with $E_{p 0}=E_{k 0}=0$,
- We have

$$
\underbrace{}_{\text {ex,1 } \rightarrow 0, \text { batch }}=-\left(U_{0}-E_{1}\right)+T_{0}\left(S_{0}-S_{1}\right)-p_{0}\left(v_{0}-v_{1}\right))
$$

- $\mathrm{W}_{\mathrm{ex}, 1 \rightarrow 2, \text { batch }}$


$$
\mathrm{W}_{\mathrm{ex}, 1 \rightarrow 2}=\mathrm{W}_{\mathrm{ex}, 1 \rightarrow 0}-\mathrm{W}_{\mathrm{ex}, 2 \rightarrow 0}
$$

$$
W_{\text {ex, } 1 \rightarrow 2, \text { batch }}=-\left(E_{2}-E_{1}\right)+T_{0}\left(S_{2}-S_{1}\right)-p_{0}\left(v_{2}-v_{1}\right)
$$

$$
\mathrm{U}_{2}+\mathrm{E}_{\mathrm{p} 2}+\mathrm{E}_{\mathrm{k} 2}
$$

- Actual and lost work in real changes, batch system
recall $W_{\text {ex, } 1 \rightarrow 2, \text { batch }}=-\left(E_{2}-E_{1}\right)+T_{0}\left(S_{2}-S_{1}\right)-p_{0}\left(v_{2}-v_{1}\right)$
rearrange $\left(E_{2}-E_{1}\right)=T_{0}\left(S-S_{2}\right)-w_{\text {ex, } 1 \rightarrow 2, \text { batch }}-p_{0}\left(v_{2}-v_{1}\right)$

| do not depend |
| :--- |
| on the path | 1st law : $\Delta E_{1 \rightarrow 2}=Q_{\text {actual }}-W_{\text {tosurr }}+W_{\text {actual }}^{\text {tosurr }}$ dWh total $\left(d W_{\text {sh }}+d W_{0}\right)+p_{0} d v$.

$=T_{0}\left(S_{2}-S_{1}\right)-Q_{\text {actual }}+\left(W_{\text {sh }}+W_{0}\right)_{\text {actural }}+\int p_{0} d v-p_{0}\left(v_{2}-v_{1}\right)$
$=T_{0}\left(S_{2}-S_{1}\right)+T S_{\text {su }}+\left(W_{\text {sh }}+W_{0}\right)_{\text {actura }}$
then $W_{\text {sh,lost }, 1 \rightarrow 2}=W_{\text {ex, } 1 \rightarrow 2}-W_{\text {sh,actual, } 1 \rightarrow 2}$

$$
\begin{aligned}
& =\mathrm{T}_{0}\left(\mathrm{~S}_{2}-\mathrm{S}_{1}\right)+\mathrm{T}_{0} \Delta \mathrm{~S}_{\text {surr }} \\
& =\mathrm{T}_{0} \Delta \mathrm{~S}_{\text {syst }}+\mathrm{T}_{0} \Delta \mathrm{~S}_{\text {surr }}
\end{aligned}
$$

$$
\mathrm{W}_{\text {sh,lost }}=\mathrm{T}_{0} \Delta \mathrm{~S}_{\text {total }}
$$

## Example I

- The little community of East Zilch, TX owns an enormous underground reservoir-not of oil, not of natural gas, but of waste gas (volume of gas in reservoir $=10^{12} \mathrm{~m}^{3}, \mathrm{c}_{\mathrm{p}}=36 \mathrm{~J} / \mathrm{mol} / \mathrm{K}, \mathrm{p}=9.95 \mathrm{~atm}$, $\mathrm{T}=237^{\circ} \mathrm{C}, \mathrm{m} \omega=0.03 \mathrm{~kg} / \mathrm{mol}$ ).
- Ideally, how much useful work can be gotten from this gas?
- If East Zilch can sell electricity to the power company at $3.6 \$ / \mathrm{kW} / \mathrm{hr}$, and if their energy extraction plant is $10 \%$ efficient, want is the value of the gas in the reservoir?
- This is a batch of gas,

Reservoir is under ground, it is certainly not zero, but Assume to be negligible

$$
\stackrel{\text { Recall }}{\stackrel{0}{0}}
$$

$$
W_{e x, 1 \rightarrow 0}=-\left[n c_{v}\left(T_{0}-T_{1}\right)\right]+T_{0} n\left(c_{p} \ln \frac{T_{0}}{T_{1}}-R \ln \frac{p_{0}}{p_{1}}\right)-p_{0}\left(v_{0}-v_{1}\right)
$$

$$
\begin{aligned}
& \mathrm{n}=\frac{\mathrm{p}_{1} \mathrm{v}_{1}}{\mathrm{RT}_{1}}=2.378 \times 10^{14} \mathrm{~mol} \\
& \mathrm{c}_{\mathrm{v}}=36-8.314=27.686 \mathrm{~J} / \mathrm{mol} \cdot \mathrm{~K} \\
& \mathrm{v}_{0}=\left(10^{12}\right)\left(\frac{9.95}{1}\right)\left(\frac{300}{510}\right)=5.853 \times 10^{12} \mathrm{~m}^{3}
\end{aligned}
$$

$$
\mathrm{W}_{\mathrm{ex}, 1 \rightarrow 0}=8.9083 \times 10^{17} \mathrm{~J}
$$

$$
\$=890 \text { million }
$$

## Example II

- If $\mathrm{E}_{\mathrm{p}}$ assume not to be negligible

$$
\begin{aligned}
& E_{p, 1 \rightarrow 0}=E_{p 0}-E_{p 1}=m g\left(z_{0}-z_{1}\right)=1.3983 \times 10^{17} \mathrm{~J} \\
& W_{e x, 1 \rightarrow 0}=8.9083 \times 10^{17}-1.3983 \times 10^{17}=7.51 \times 10^{17} \mathrm{~J} \\
& \$=140 \text { million }
\end{aligned}
$$

- This means, the potential energy should not always be ignored.


## Quiz VIII

A system consists of 5 kg of water at $10^{\circ} \mathrm{C}$ and 1 bar. Determine the exergy in kJ , if the system is at rest and zero elevation relative to the reference environment for which $\mathrm{T}_{0}=20^{\circ} \mathrm{C}$, $p_{0}=1$ bar. (Use $\mathrm{H}_{2} \mathrm{O}$ property table to find necessary information)

## EXERGY IN FLOW SYSTEMS



- Recall
$\mathrm{W}_{\mathrm{ex}, 1 \rightarrow 0, \text { batch }}=-\left[\left(\mathrm{U}_{0}+\mathrm{E}_{\mathrm{p} 0}+\mathrm{E}_{\mathrm{k} 0}\right)-\left(\mathrm{U}_{1}+\mathrm{E}_{\mathrm{p} 1}+\mathrm{E}_{\mathrm{k} 1}\right)\right]+\mathrm{T}_{0}\left(\mathrm{~S}_{0}-\mathrm{S}_{1}\right)-\mathrm{p}_{0}\left(\mathrm{v}_{0}-\mathrm{v}_{1}\right)$
- Therefore,

$$
\begin{aligned}
& W_{\text {ex }, 1 \rightarrow 0}=-\left[\left(H+E_{p}+E_{k}\right)_{0}-\left(H+E_{p}+E_{k}\right)_{1}\right]+T_{0}\left(S_{0}-S_{1}\right) \\
& W_{\text {ex }, 1 \rightarrow 2}=-\left[\left(H+E_{p}+E_{k}\right)_{2}-\left(H+E_{p}+E_{k}\right)_{1}\right]+T_{0}\left(S_{2}-S_{1}\right)
\end{aligned}
$$

- Recall

- Recap

$$
\mathrm{W}_{\mathrm{ex}, 1 \rightarrow 0}=\mathrm{W}_{\mathrm{ex}, 2 \rightarrow 0}+\mathrm{W}_{\mathrm{sh}, \text { attual }, 1 \rightarrow 2}+\mathrm{W}_{\mathrm{sh}, \text { ost }, 1 \rightarrow 2}
$$

## Example III


surroundings
$\mathrm{T}_{0}=300 \mathrm{~K}$
$\mathrm{p}_{0}=1 \mathrm{bar}$

- A stream of $2 \mathrm{~mol} / \mathrm{s}$ of air goes from 1000 K and 10 bar to 500 K and 5 bar while doing 5.0 kW of work. Surroundings are 300 K and 1 bar. What is the lost work for this process?
- Recall

$$
\begin{aligned}
& W_{e x, 1 \rightarrow 2}=-\left[\left(H+E_{p}+E_{k}\right)_{2}-\left(H+E_{p}+E_{k}\right)_{1}\right]+T_{0}\left(S_{2}-S_{1}\right) \\
& w_{e x, 1 \rightarrow 2}=-\left[h_{2}-h_{1}\right]+T_{0}\left(s_{2}-s_{1}\right) \\
& =c_{p}\left(T_{1}-T_{2}\right)+T_{0}\left(c_{p} \ln \frac{T_{2}}{T_{1}}-R \ln \frac{p_{2}}{p_{1}}\right) \\
& =10228 \mathrm{~J} / \mathrm{mol}
\end{aligned}
$$

- Available power

$$
\dot{\mathrm{W}}_{\mathrm{ex}, 1 \rightarrow 2}=(10228)(2)=20.5 \mathrm{~kW}
$$

- The actual power production is 5 kW , so

$$
\dot{\mathrm{W}}_{\text {sh,lost }}=20.5-5.0=15.5 \mathrm{~kW}
$$

## Example IV

- Saudi Arabia, a hot dry country ( $\mathrm{T}_{\mathrm{ave}}=30^{\circ} \mathrm{C}$ ), plans to lasso icebergs in Antarctica, two them to Jiddah Harbor, melt and store the water at $5^{\circ} \mathrm{C}$, and thereby supply the country with fresh water. But one can produce work, electricity, and air conditioning in addition to fresh water during the melting process. If they do not try to recover this available work, how much power do they waste if they bring in a $10^{6}$ ton iceberg every three weeks?

- Since we are only interested in the overall $1 \rightarrow 3$ change, we can bypass state 2.
- Consider this to be a steady state, $\Delta \mathrm{E}_{\mathrm{p}}=\Delta \mathrm{E}_{\mathrm{k}}=0$
- Therefore,

$$
w_{e x, 1 \rightarrow 3}=-\left[\left(h+e_{p}+e_{k}\right)_{3}-\left(h+e_{p}+e_{k}\right)_{1}\right]+T_{0}\left(s_{3}-s_{1}\right)
$$

- From the reference tables
$\mathrm{h}_{1}=-333.43 \mathrm{~kJ} / \mathrm{kg} \quad \mathrm{h}_{3}=20.98 \mathrm{~kJ} / \mathrm{kg}$
$\mathrm{s}_{1}=-1.221 \mathrm{~kJ} / \mathrm{kg} / \mathrm{K} \quad \mathrm{s}_{3}=0.0761 \mathrm{~kJ} / \mathrm{kg} / \mathrm{K}$
- Hence,

$$
\begin{aligned}
\mathrm{w}_{\text {ex, } 1 \rightarrow 3} & =38.61 \mathrm{~kJ} / \mathrm{kg} \\
\mathrm{w}_{\text {lost }} & =38.61 \mathrm{~kJ} / \mathrm{kg} \quad \mathrm{w}_{\text {ex }}=\mathrm{w}_{\text {lost }}+\mathrm{w}_{\text {actual }} \\
\dot{\mathrm{W}}_{\text {lost }} & =(38.61)\left(\frac{1000 \mathrm{~kg}}{\text { ton }}\right)\left(\frac{10^{6} \text { tons }}{21 \text { days }}\right)\left(\frac{1 \text { day }}{24 \times 3600 \mathrm{~s}}\right) \\
& =21280 \frac{\mathrm{~kJ}}{\mathrm{~s}}=21.3 \mathrm{MW}
\end{aligned}
$$

## recap

- The availability of heat (exergy of heat)


$$
\begin{aligned}
& \mathrm{w}_{\text {carnot }}=\mathrm{Q}-\mathrm{Q}_{0} \\
& \mathrm{w}_{\text {carnot }}=\int \mathrm{Tds}-\int \mathrm{T}_{0} \mathrm{ds} \\
& \mathrm{Ex}_{\text {heat }}=\left\{\begin{array}{l}
\mathrm{Td} s-\int \mathrm{T}_{0} \mathrm{ds} \\
\Delta \mathrm{Ex}_{\text {heat }}=Q_{\text {ev }}-\int T_{0} d s
\end{array} 2^{\text {nd law }}\right.
\end{aligned}
$$

- The availability of work (exergy of work)

$$
\Delta E x_{\text {work }}=W_{\text {rev }}-\int p_{0} d v
$$

- The total exergy is that exergy that can be extracted through heat and work processes

$$
\Delta E x_{\text {system }}=\Delta E x_{\text {heat }}-\Delta \mathrm{Ex}_{\text {work }}
$$

- exergy of the system becomes

$$
\begin{aligned}
& \Delta E x_{\text {system }}=\left(Q_{\text {rev }}-T_{0} \int d s\right)-\left(W_{\text {rev }}-\int p_{0} d v\right) \\
&=\left(Q_{\text {rev }}-W_{\text {rev }}\right)-\left(T_{0} \int d s-\int p_{0} d v\right) \\
& \Delta E x_{\text {system }}=\Delta E-\left(T_{0} \int d s-\int p_{0} d v\right)
\end{aligned}
$$

- Finally $\Delta E x_{\text {system }}=\Delta U-\int p_{0} d v-T_{0} \int d s+\Delta e_{p}+\Delta e_{k}$
- Closed: $W_{\text {ex, } 1 \rightarrow 0, \text { batch }}=-\left(U_{0}-E_{1}\right)+T_{0}\left(S_{0}-S_{1}\right)-p_{0}\left(v_{0}-v_{1}\right)$
- Flow: $\mathrm{W}_{\text {ex, } 1 \rightarrow 0}=-\left[\left(\mathrm{H}+\mathrm{E}_{\mathrm{p}}+\mathrm{E}_{\mathrm{k}}\right)_{0}-\left(\mathrm{H}+\mathrm{E}_{\mathrm{p}}+\mathrm{E}_{\mathrm{k}}\right)_{1}\right]+\mathrm{T}_{0}\left(\mathrm{~S}_{0}-\mathrm{S}_{1}\right)$


## Exergy

- In distillation columns, this work is supplied by heat being injected at the reboiler $\mathrm{q}_{\text {reb }}$ and rejected at the condenser $\mathrm{q}_{\text {cond }}$. The net work available from the heat energy (or the net exergy from the heat transferred) is:

$$
E_{\text {neat }}=q_{\text {reb }}\left(1-\frac{T_{0}}{T_{\text {reb }}}\right)-q_{\text {cond }}\left(1-\frac{T_{0}}{T_{\text {cond }}}\right)
$$

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## Para－Xylene Expansion



## Assess if the waste heat from the toluene tower is enough



Multi effect propane-hydrocarbon absorption refrigeration system
Chinese Patent (Granted) 200910056897.9B


